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**HW Pre Calculus 12: Section 1.2 Horizontal and Vertical Translations**

1. Suppose you are given a function  $f(x) = 3(x-4)^2 + 5$  and you replace the variable "x" in the equation with  $x+3$ , then answer the following:
  - i) What does the equation become after the transformation?
  - ii) Which way if the graph shifted and by how much?
  - iii) Where is the vertex of the parabola after the transformation?
2. Suppose you are given a function  $f(x) = 2x^3 - 8x^2 + 5$  and you replace the variable "x" in the equation with  $x-2$  and the "y" variable with  $y+10$ , then answer the following:
  - i) What does the equation become after the transformations? Simplify your equation & isolate the "Y" variable.
  - ii) Which way if the graph shifted and by how much?
3. Indicate the transformation from the function on the left to the function on the right:
  - a)  $y = x^2 + 3x + 4 \rightarrow y = (x-5)^2 + 3(x-5) + 4$
  - b)  $y = x^2 + 4x + 5 \rightarrow y = x^2 + 4x + 11$
  - c)  $y = \sqrt{3x-4} \rightarrow y = \sqrt{3x-4} + 10$
  - d)  $y = \sqrt{3x-4} \rightarrow y = \sqrt{3x-7}$
  - e)  $y = |x| \rightarrow y = |x-2| + 4$

f)  $y = \sqrt{x} \rightarrow y = \sqrt{x+3} - 7$

g)  $y = 3x + 2 \rightarrow y = 3x + 8$

h)  $y = x^2 \rightarrow y = x^2 + 6x + 12$

i)  $y = \frac{1}{x} \rightarrow y = \frac{1}{x+5} + 3$

4. Given each equation for  $y = f(x)$ , indicate the new equation after each translation:

a.  $f(x) = 3x - 5$  A horizontal shift of 3 units right and 2 units up

b.  $f(x) = 2x^2 + 3$  A horizontal shift of 5 units left and 8 units up

c.  $f(x) = \sqrt{x-5} + 1$  A horizontal shift of 7 units right and 6 units down

d.  $f(x) = 3^x + 2$  A horizontal shift of 11 units left and 2 units down

e.  $x^2 + y^2 = 16$  A horizontal shift of 4 units right and 8 units up

f)  $f(x) = \frac{1}{x-3}$  A horizontal shift of 2 units left and 6 units down

g)  $f(x) = x^3 + 2x^2$  A horizontal shift of 5 units right and 11 units down

5. Given the graph of  $y = f(x)$ , draw the resulting image after each transformation:

	i) $y = f(x-3)+1$ 	ii) $y-3 = f(x+1)$ 
	i) $y+1 = f(x+2)$ 	ii) $y = 1 + f(x+4) - 2$ 
	i) $y-3 = f(x-4)$ 	ii) $y-2 = f(x+3)-5$ 

6. Given that the coordinates of  $(2,3)$  is transformed to  $(8,4)$  from  $y = f(x) \rightarrow y = f(x-a)+b$ , what is the value of  $a+b$ ?

7. Given that the coordinates (a,b) are on the function  $y = f(x)$ , find the new coordinates for each function after the transformation:

i) $y = f(x-3)+2$	ii) $y-5 = f(x+1)+2$
iii) $y = f(x+7)-11$	iv) $y-4 = f(x-5)+3$

8. Suppose the point (a,b) is on the function from the left. What will the point become after the transformation shown from the function on the right? Indicate all possible answers:

a)  $y = |3x-2| \rightarrow f(x) = |3x+12|+4$

b)  $y = \frac{4}{3}x+11 \rightarrow f(x) = \frac{4x+10}{3}$

c)  $y = 2^x + 1 \rightarrow f(x) = 4(2^x) - 3$

d)  $y = \frac{1}{x} \rightarrow f(x) = -1 - x - x^2 - x^3 + \dots \quad \{0 < x < 1\}$

9. The parabola  $y = x^2 - 4x + 3$  is translated 5 units right. In this new position, the equation of the parabola is  $y = x^2 - 14x + d$ . What is the value of "d"?