

Math 9 Enriched  
Final Exam Review

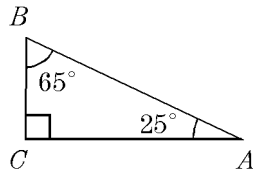
Name \_\_\_\_\_

Date \_\_\_\_\_

1. In  $\triangle ABC$ ,  $m\angle C = 90^\circ$ ,  $AC = 3$ ,  $BC = 4$ , and  $AB = 5$ . Find  $\cos \angle A$ .

3. Find  $\sin 32^\circ$ .

5. Find  $\sin \angle A$ .



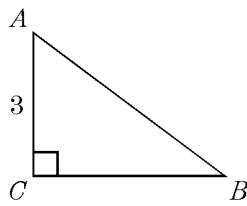
2. In  $\triangle ABC$ ,  $m\angle C = 90^\circ$ ,  $AC = 3$ ,  $BC = 4$ , and  $AB = 5$ . Find  $\cot \angle B$ .

4. Find  $\tan 45^\circ$ .

6. Find  $\cos \angle A$ .

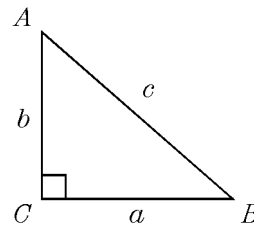
7. If  $\sin \theta = \frac{5}{7}$ , find  $\theta$  to the nearest degree.

9. If  $\sin \angle B = \frac{3}{4}$ , find  $AB$ .



8. If  $\tan \angle K = \frac{7}{10}$ , find  $m\angle K$  to the nearest degree.

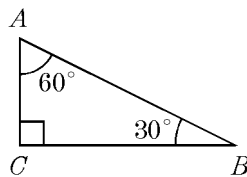
10. If  $a = 7$  and  $b = 9$ , find  $m\angle A$  to the nearest tenth of a degree.



11. Find  $\sin 30^\circ$ .

13. Find  $\sin 45^\circ$ .

15. If  $AC = 1$ , find  $BC$ .



12. Find  $\sin 60^\circ$ .

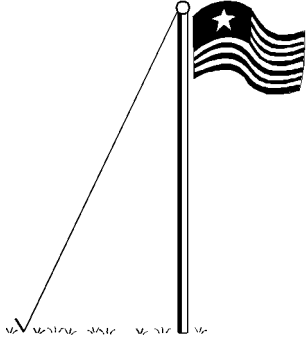
14. Find  $\cos 30^\circ$ .

16. If  $AB = 2$ , find  $BC$ .

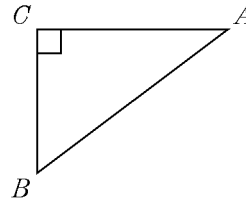
17. When an 11 foot 11 inches tall tree casts a 10 inch long shadow, what is the angle of elevation of the sun?

18. If  $\cos \angle F = \frac{4}{5}$ , find  $\tan \angle F$ .

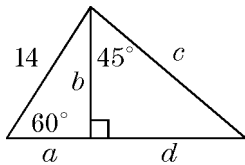
19. A wire 32 feet long is attached to the top of a flagpole 23 feet long. Approximately what is the measure of the angle the wire makes with the ground? Round your answer to the nearest tenth of a degree or nearest ten minutes.



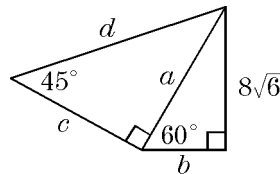
20. Solve the right triangle if  $\angle A = 41^\circ$  and  $b = 12.5$  centimeters. Give lengths to 3 significant figures and angles to the nearest tenth of a degree.



21. Find the exact value of each labelled part in the figure.



22. Find the exact value of each labelled part in the figure.



23.  $b = 45$ ,  $\alpha = 56^\circ$ ,  $\beta = 72^\circ$

25.  $a = 9$ ,  $b = 12$ ,  $\alpha = 47^\circ$

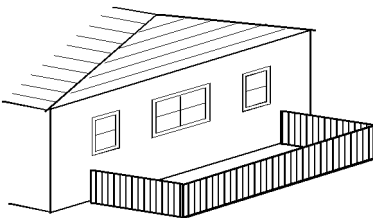
27.  $a = 4$ ,  $b = 5$ ,  $\gamma = 30^\circ$

24.  $b = 27$ ,  $a = 54$ ,  $\beta = 30^\circ$

26.  $a = 6.9$ ,  $c = 11.4$ ,  $\beta = 141^\circ$

28. Two fire towers, at points  $A$  and  $B$ , are on a lakeshore 40 kilometers apart. Each has visual contact with a ranger at point  $C$ . If  $m\angle CAB = 20^\circ 30'$  and  $m\angle CBA = 110^\circ$ , how far is the ranger from point  $A$ ?

29. A rectangular patio is surrounded on three sides by a fence (the remaining side is up against the house). If the area of the patio is  $38\text{m}^2$ , and the total length of fence is 18m, what is the length and width of the patio?



30. The equation of the axis of symmetry of a parabola is  $x + 2 = 0$  and one point on the graph is  $\mathbf{P}(5, 3)$ . Find another point on the graph.

31. A rectangular swimming pool is 12 meters long and 8 meters wide. It is surrounded by a cement walkway of uniform width. The area of the walkway is twice the area of the pool. How wide is the walkway?

Simplify.

$$32. \sqrt[3]{8a^3}$$

$$34. \sqrt[3]{\frac{-125x^5y^4z^7}{8x^2y^{10}z^4}}$$

$$36. -\frac{5}{2}\sqrt{40} \cdot 3\sqrt{60}$$

$$38. \sqrt{8a^5}(-\sqrt{2a^3})$$

$$40. 2cd\sqrt{5c^3d} \cdot \sqrt{55cd^2}$$

$$42. \frac{8\sqrt{11}}{3\sqrt{5}}$$

$$44. \frac{\sqrt[3]{8}}{\sqrt[5]{-32}}$$

$$46. \frac{3e^4f^7}{\sqrt{12e^2f^3}}$$

$$48. -\sqrt{121} + \sqrt{144} - \sqrt{49}$$

$$50. \sqrt{49e^2} + \sqrt{64e^3}$$

$$52. -3y\sqrt[5]{64y^6} - 2\sqrt[5]{486y^{11}}$$

Factor.

$$53. 162 - 45x + 3x^2$$

$$55. 4m^2 - 324$$

$$57. 2(k-4) - k(k-4) + k^2(k-4)$$

$$59. 216z^3 - 125a^3$$

Solve.

$$61. 0 = p^2 + 5p + 2$$

$$63. 2x - 3x^2 = -2x - 12$$

Simplify (assume variable expressions are positive).

$$64. (x^3 - x^2 - 17x + 12) \div (4 + x)$$

$$33. -\sqrt[5]{\frac{1024a^5b^{10}}{16,807}}$$

$$35. \sqrt[3]{\sqrt[3]{512m^9n^{18}}}$$

$$37. \left(-\frac{2\sqrt{15}}{3}\right)(2\sqrt{30})(-\sqrt{45})$$

$$39. \sqrt{33c^2d} \cdot \sqrt{66d^5c^5}$$

$$41. \sqrt{3a+6} \cdot \sqrt{3a-6}$$

$$43. \sqrt{\frac{1}{5}} \cdot \sqrt{\frac{2}{3}}$$

$$45. \frac{5n}{\sqrt{15n}}$$

$$47. \frac{\sqrt{x-y}}{\sqrt{x^2y-xy^2}}$$

$$49. 2\sqrt{80} - 3\sqrt{45} + 3\sqrt{245}$$

$$51. -3cd\sqrt{75c} + 2\sqrt{12c^3d^2}$$

$$54. 35cb^2 - 14cb - 21c$$

$$56. m^4 - 98m^2 + 2401$$

$$58. 27 - 64y^3$$

$$60. 64 - w^6$$

$$62. a^2 + 7a = 15$$

$$65. (7x^4 - 5x^3 + 35x^2 - 46x + 15) \div (7x - 5)$$

Solve by completing the square.

66.  $m^2 + 6m = -7$

68. Factor  $x^{6y} - y^{9x}$  completely.

70. Simplify: 
$$\frac{\sqrt{x} - \frac{1}{\sqrt{x}}}{\frac{1 - \sqrt{x}}{\sqrt{x}}} =$$

Find the slope.

71.  $(\frac{1}{2}, -3)$   $(4\frac{1}{2}, 0)$

73.  $(\frac{3}{4}, \frac{1}{3})$   $(-\frac{1}{4}, \frac{1}{6})$

75.  $(p - 1, -8p)$   $(9p - 1, 7p)$

77. A segment has endpoints at  $(k, k + 4)$  and  $(8 - k, k + 2)$ . What is the midpoint?

79. Given  $K(0, 5)$ ,  $M(-1, -2)$  and  $N(7, 10)$ . Write the equation of the line which passes through  $K$  and the midpoint of  $\overline{MN}$ .

81. Given  $E(-7, 4)$  and  $F(1, -8)$ . Write the equation of the line which is perpendicular to  $\overline{EF}$  and contains the midpoint of  $\overline{EF}$ .

Solve.

82.  $3x - y = 0$   
 $5x + 5 = 0$

84.  $x - y + 4 = 0$   
 $-2x + y - 8 = 0$

86.  $y = x^2 + 2$   
 $y = -3x + 2$

88.  $a - 2b + c + d - e = 4$   
 $a - c - d = 1$   
 $b + c + e = -2$   
 $2a - c + 2d = 12$   
 $a + 2b + d + e = 4$

90.  $3 + \frac{1}{4}(7 - 3n) \geq \frac{1}{3}(2 - 3n) + 4$

67.  $3z^2 + 12z + 15 = 0$

69. Factor  $(x^2 + 2x)^2 - 11(x^2 + 2x) + 24$  completely.

72.  $(2x, y)$   $(7x, 2y)$

74.  $(a + b, b)$   $(a - b, -b)$

76. contains  $(2, -2)$  and  $(-6, 1)$

78. What are the  $x$ - and  $y$ -intercepts of the line:  
 $-5x + 16y - 6 = 0$ ?

80. Given  $A(0, -3)$ ,  $B(3, 8)$  and  $C(-2, 5)$ . Write the equation of the line which passes through  $B$  and is parallel to  $\overleftrightarrow{AC}$ .

83.  $y = -\frac{1}{3}x$   
 $x + 6y + 9 = 0$

85.  $\frac{y + 4}{x - 4} = \frac{7}{3}$   
 $\frac{y - 4}{x} = -\frac{1}{7}$

87.  $-2x + 5y - z = -4$   
 $4x - 5y + z = 9$   
 $2x + 10y + 3z = 12$

89.  $18 + 6c \geq 4c - 5$

91. A triangle has vertices  $(-5, -2)$ ,  $(2, -2)$ , and  $(-5, 3)$ . Find the perimeter of the triangle.

92. For what value(s) of  $k$  are the points  $(k + 3, -6)$ ,  $(5, k - 7)$ , and  $(2, 2)$  collinear?
93. A tower 52 m high can be seen from a point  $\mathbf{P}$  on a level with the foot of the tower. If the angle of elevation to the top of the tower is  $38^\circ$ , then how far is  $\mathbf{P}$  from the base of the tower? Answer to 1 decimal place.
94. If  $\sin \theta = \frac{2}{3}$  then what is the  $\tan \theta$ ?

**Answer List**

- |  |   |  |
|--|---|--|
| 1. $\frac{3}{5}$   | 2. $\frac{4}{3}$  | 3. 0.5299  |
| 4. 1.000   | 5. 0.4226   | 6. 0.9063  |
| 7. $46^\circ$  | 8. $35^\circ$   | 9. 4   |
| 10. $37.9^\circ$   | 11. $\frac{1}{2}$   | 12. $\frac{\sqrt{3}}{2}$   |
| 13. $\frac{\sqrt{2}}{2}$   | 14. $\frac{\sqrt{3}}{2}$  | 15. $\sqrt{3}$   |
| 16. $\sqrt{3}$   | 17. $\approx 86^\circ$  | 18. $\frac{3}{4}$  |
| 19. $46.0^\circ$   | 20. $\angle B = 49.0^\circ$ , $a \approx 10.9$ cm,<br>$c \approx 16.6$ cm | 21. $a = 7$ , $b = 7\sqrt{3}$ , $c = 7\sqrt{6}$ ,<br>$d = 7\sqrt{3}$ |
| 22. $a = 16\sqrt{2}$ , $b = 8\sqrt{2}$ , $r = 16\sqrt{2}$ ,<br>$s = 32$  | 23. $\gamma = 52^\circ$ , $c = 37.3$ , $a = 39.2$                         | 24. $c = 27\sqrt{3}$ , $\alpha = 90^\circ$ , $\gamma = 60^\circ$     |
| 25. $c = 10.18$ , $\beta = 77.2^\circ$ , $\gamma = 55.8^\circ$<br>or $c = 6.19$ , $\beta = 102.8^\circ$ ,<br>$\gamma = 30.2^\circ$ | 26. $b = 17.3$ , $\alpha = 14.5^\circ$ , $\gamma = 24.5^\circ$            | 27. $\alpha = 52.5^\circ$ , $\beta = 97.5^\circ$ , $c = 2.5$         |
| 28. 49.43 km   | 29. about $11.2 \times 3.4$ m   | 30. $(-9, 3)$  |
| 31. $\approx 3.5$ m  | 32. $2a$  | 33. $\frac{-4ab^2}{7}$   |
| 34. $\frac{-5xz}{2y^2}$  | 35. $2mn^2$   | 36. $-150\sqrt{6}$   |
| 37. $60\sqrt{10}$  | 38. $-4a^4$   | 39. $33d^3c^3\sqrt{2c}$  |
| 40. $10c^3d^2\sqrt{11d}$   | 41. $3\sqrt{a^2 - 4}$   | 42. $\frac{8\sqrt{55}}{15}$  |
| 43. $\frac{\sqrt{30}}{15}$   | 44. $-1$  | 45. $\frac{\sqrt{15n}}{3}$   |
| 46. $\frac{e^3f^5\sqrt{3f}}{2}$  | 47. $\frac{\sqrt{xy}}{xy}$  | 48. $-6$   |
| 49. $20\sqrt{5}$   | 50. $7e + 8e\sqrt{e}$   | 51. $-11cd\sqrt{3c}$   |
| 52. $-12y^2\sqrt[3]{2y}$   | 53. $3(6 - x)(9 - x)$   | 54. $7c(b - 1)(5b + 3)$  |
| 55. $4(m + 9)(m - 9)$  | 56. $(m + 7)^2(m - 7)^2$  | 57. $(k - 4)(2 - k + k^2)$   |
| 58. $(3 - 4y)(9 + 12y + 16y^2)$  | 59. $(6z - 5a)(36z^2 + 30az + 25a^2)$                                     | 60. $(4 - w^2)(16 + 4w^2 + w^4)$                                     |
| 61. $\frac{-5 \pm \sqrt{17}}{2}$   | 62. $\frac{-7 \pm \sqrt{109}}{2}$   | 63. $\frac{2 \pm 2\sqrt{10}}{3}$                                     |
| 64. $x^2 - 5x + 3$   | 65. $x^3 + 5x - 3$  | 66. $-3 \pm \sqrt{2}$  |
| 67. $\emptyset$  | 68. $(x^{2y} - y^{3x})(x^{4y} + x^{2y}y^{3x} + y^{6x})$                   | 69. $(x - 1)(x - 2)(x + 3)(x + 4)$                                   |
| 70. $-(1 + \sqrt{x})$  | 71. $\frac{3}{4}$   | 72. $\frac{y}{5x}$   |
| 73. $(\frac{1}{4}, \frac{1}{4})$   | 74. $(a, 0)$  | 75. $17p$  |
| 76. $y = -\frac{3}{8}x - \frac{5}{4}$  | 77. $(4, k + 3)$  | 78. $-\frac{6}{5}$ and $\frac{3}{8}$                                 |
| 79. $y = -\frac{1}{3}x + 5$  | 80. $y = -4x + 20$  | 81. $y = \frac{2}{3}x$   |
| 82. $(-1, -3)$   | 83. $(9, -3)$   | 84. $(-4, 0)$  |
| 85. $(7, 3)$   | 86. $(0, 2)$ and $(-3, 11)$   | 87. $(\frac{5}{2}, \frac{2}{5}, 1)$                                  |
| 88. $(2, -1, -2, 3, 1)$  | 89. $c \geq -\frac{23}{2}$  | 90. $n \geq -\frac{1}{3}$  |
| 91. $12 + \sqrt{74}$   | 92. 3, 5  | 93. 66.6 m   |
| 94. $\pm \frac{2}{\sqrt{5}}$   |   |  |

## Catalog List

1. TRI MB 2
2. TRI MB 12
3. TRI MC 1
4. TRI MC 21
5. TRI MC 61
6. TRI MC 62
7. TRI ME 15
8. TRI ME 21
9. TRI MF 1
10. TRI MG 25
11. TRI MH 1
12. TRI MH 2
13. TRI MH 3
14. TRI MH 4
15. TRI MI 1
16. TRI MI 34
17. TRI ML 15
18. TRI MK 7
19. TRI ML 3
20. TRI MJ 4
21. TRI OH 53
22. TRI OH 56
23. TRI QF 1
24. TRI QF 17
25. TRI QF 45
26. TRI QG 15
27. TRI QG 33
28. TRI QK 1
29. ALG NH 33
30. CM1 ME 55
31. ALG NH 43
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36. TRI BC 39
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43. TRI BD 65
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64. TRI GA 27
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67. ALG NC 62
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69. CM1 AC 73
70. CM1 BC 55
71. ALG PA 55
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74. ALG PB 55
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